

Solve the system using Linear Combination.

$$\begin{array}{rcl}
 1) & 2(8x + 9y = 15) & 16x + 18y = 30 \\
 & 9(5x - 2y = 17) & 45x - 18y = 153 \\
 \hline
 & & 61x = 183 \\
 & & x = 3 \\
 \hline
 & 5(3) - 2y = 17 & \\
 & 15 - 2y = 17 & \\
 & -15 & -15 \\
 & -2y = 2 & \\
 & y = -1 &
 \end{array}$$

Warm-up

$$(3, -1)$$

Solve the system using Substitution.

$$\begin{array}{rcl}
 2) & x - 2y = 4 & x = 2y + 4 \\
 & 3x - 6y = 8 & 3(2y + 4) - 6y = 8 \\
 & & 6y + 12 - 6y = 8 \\
 & & 12 = 8 \\
 & & \text{No solution}
 \end{array}$$

Solving Linear Systems
Application Problems
-Set up each problem

Homework Questions:

- 10.) $(-6, 5)$
- 1.) $(2.33, -0.33)$
- 2.) $(2.71, 9.57)$
- 3.) $(11.08, 16.25)$
- 4.) $(24, -43)$
- 4.) $(4, 4)$
- 18.) many solutions

- 14.) length 30
width 15
- 15.) 35, 55
- 16.) 60, 120

- 1.) 6lbs \$1.10 coffee
14lbs \$0.80 coffee
- 2.) 25lbs \$1.16 tea
35lbs \$0.92 tea
- 3.) 12lbs \$0.70 chips
18lbs \$0.90 chips
- 4.) 11 nickels, 6 pennies
- 5.) 11 quarters, 5 dimes
- 6.) 14 dimes, 7 nickels
- 7.) 18, -7
- 8.) 9, 27
- 9.) 12, 7
- 10.) 38, 56
- 11.) \$1600 at 2%
\$4800 at 4%
- 12.) \$4000 at 6%
\$4600 at 5%
- 13.) \$3500 at 5%
\$1200 at 4.5%

Bonus

Find the vertex of the following quadratic

$$y=-(x-4)^2+7$$

- A. (4,-7)
- B. (-4,7)
- C. (4, 7)
- D. (-4, -7)

Algebra 2 Trig Daily Learning Target Quiz
Unit 4 - Day 2

1.) Solve by graphing:

$$y = -x + 5$$
$$-2x + 3y = 0$$

2.) Solve by substitution:

$$8x + 2y = 2$$
$$x + 3y = 14$$

3.) Solve by elimination:

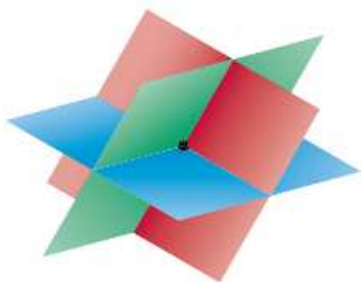
$$7x - 3y = 6$$
$$-2x + 5y = -10$$

4.) A vendor sold 200 tickets for an upcoming rock concert. Floor seats were \$36 and stadium seats were \$28. The vendor sold \$6080 in tickets. How many floor seats and how many stadium seats were sold?

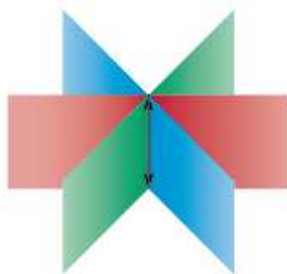
Chapter 3 Systems (3.4)3 Variable Systems

Exactly one solution

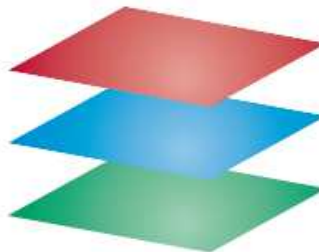
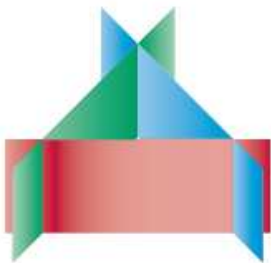
The planes intersect in a single point.

**Infinitely many solutions**

The planes intersect in a line or are the same plane.

**No solution**

The planes have no common point of intersection.



KEY CONCEPT*For Your Notebook***The Elimination Method for a Three-Variable System**

- STEP 1** Rewrite the linear system in three variables as a linear system in two variables by using the elimination method.
- STEP 2** Solve the new linear system for both of its variables.
- STEP 3** Substitute the values found in Step 2 into one of the original equations and solve for the remaining variable.

If you obtain a false equation, such as $0 = 1$, in any of the steps, then the system has no solution.

If you do not obtain a false equation, but obtain an identity such as $0 = 0$, then the system has infinitely many solutions.

Notes Sheet

$$\begin{aligned} \textcircled{1} \quad & 2x - y + \underline{z} = 4 \\ \textcircled{2} \quad & x + 3y - \underline{z} = 11 \\ \textcircled{3} \quad & 4x + y - \underline{z} = 14 \end{aligned}$$

$$\begin{aligned} \textcircled{1} + \textcircled{2} \\ 2x - y + \cancel{z} &= 4 \\ x + 3y - \cancel{z} &= 11 \\ \hline \textcircled{4} \quad 3x + 2y &= 15 \end{aligned}$$

$$\begin{aligned} \textcircled{1} + \textcircled{3} \\ 2x - y + \cancel{z} &= 4 \\ 4x + y - \cancel{z} &= 14 \\ \hline \textcircled{5} \quad 6x &= 18 \\ x &= 3 \end{aligned}$$

$$\begin{aligned} \textcircled{4} \quad 3(3) + 2y &= 15 \\ 9 + 2y &= 15 \\ 2y &= 6 \\ y &= 3 \end{aligned}$$

$$\begin{aligned} \textcircled{1} \quad 2x - y + z &= 4 \\ 2(3) - 3 + z &= 4 \\ 6 - 3 + z &= 4 \\ z &= 1 \end{aligned}$$

$$\begin{matrix} x & y & z \\ (3, & 3, & 1) \end{matrix}$$

Solve.

 $(2, -1, 1)$

$$\textcircled{1} \textcircled{x} + 2y - 3z = -3$$

$$\textcircled{2} 2x - 5y + 4z = 13$$

$$\textcircled{3} \textcircled{5x} + 4y - z = 5$$

Example

$$\begin{aligned} x + 2(-1) - 3(1) &= -3 \\ x - 2 - 3 &= -3 \\ x - 5 &= -3 \\ x &= 2 \end{aligned}$$

$$-2 \textcircled{1} + \textcircled{2}$$

$$-2x - 4y + 6z = 6$$

$$2x - 5y + 4z = 13$$

$$\textcircled{4} -9y + 10z = 19$$

$$\begin{array}{r} 14 \\ 42 \\ \hline 56 \end{array}$$

cancel
same
variable

$$-5 \textcircled{1} + \textcircled{3}$$

$$-5x - 10y + 15z = 15$$

$$5x + 4y - z = 5$$

$$\textcircled{5} -6y + 14z = 20$$

Cancel y

$$-2 \textcircled{4} + 3 \textcircled{5}$$

$$18y - 20z = -38$$

$$-18y + 42z = 60$$

$$22z = 22$$

$$z = 1$$

$$-9y + 10(1) = 19$$

$$-9y = 9$$

$$y = -1$$

Solve.

$$\textcircled{1} \underline{3x} - 2y + 4z = 20$$

$$\textcircled{2} \underline{-x} + 5y + 12z = 73$$

$$\textcircled{3} x + 3y - 2z = 1$$

Example

$$\begin{array}{r} 73 \\ \times 3 \\ \hline 219 \end{array}$$

$$\begin{array}{r} \textcircled{2} + \textcircled{3} \\ -x + 5y + 12z = 73 \\ x + 3y - 2z = 1 \\ \hline \textcircled{4} 8y + 10z = 74 \end{array}$$

cancel
x

$$\begin{array}{r} \textcircled{1} + 3\textcircled{2} \\ 3x - 2y + 4z = 20 \\ -3x + 15y + 36z = 219 \\ \hline \textcircled{5} 13y + 40z = 239 \end{array}$$

$$\begin{array}{r} 74 \\ \times 4 \\ \hline 296 \end{array}$$

$$-4\textcircled{4} + \textcircled{5}$$

$$\begin{array}{r} -32y - 40z = -296 \\ 13y + 40z = 239 \\ \hline \end{array}$$

$$(2, 3, 5)$$

$$8(3) + 10z = 74$$

$$\begin{array}{r} 24 + 10z = 74 \\ -24 \\ \hline 10z = 50 \end{array}$$

$$\begin{array}{r} 10z = 50 \\ z = 5 \end{array}$$

$$\begin{array}{r} -19y = -57 \\ \hline -19 \\ y = 3 \end{array}$$

$$\begin{array}{r} \textcircled{3} x + 3(3) - 2(5) = 1 \\ x + 9 - 10 = 1 \\ x - 1 = 1 \\ x = 2 \end{array}$$

Thanksgiving Trivia

Solve.

$$\textcircled{1} \quad 2x + 4y + 10z = 14$$

$$\textcircled{2} \quad x + 2y + 5z = -4$$

$$\textcircled{3} \quad 3x - 4y - 3z = 15$$

Example

$$\textcircled{1} + \textcircled{3}$$

$$\begin{array}{r} 2x + 4y + 10z = 14 \\ 3x - 4y - 3z = 15 \\ \hline \end{array}$$

$$\textcircled{4} \quad 5x + 7z = 29$$

$$\textcircled{4} - \textcircled{5}$$

$$\begin{array}{r} 5x + 7z = 29 \\ -5x - 7z = -7 \\ \hline \end{array}$$

$$0 = 22$$

No solution

cancel
y

$$2\textcircled{2} + \textcircled{3}$$

$$\begin{array}{r} 2x + 4y + 10z = -8 \\ 3x - 4y - 3z = 15 \\ \hline \end{array}$$

$$\textcircled{5} \quad 5x + 7z = 7$$

Example

A theater group sold a total of 440 tickets for \$3940. Each regular ticket costs \$5, each premium ticket costs \$15, and each elite ticket costs \$25. The number of regular tickets was three times the number of premium and elite tickets combined. How many of each type of ticket were sold?

$x = \text{regular}$ $y = \text{premium}$ $z = \text{elite}$

$$x + y + z = 440$$

$$5x + 15y + 25z = 3940$$

$$x = 3(y + z)$$

And your assignment:

Day 2 (3.4)

-Quiz next class

(2 variable systems, word problems,
3 variable systems)