

Integration by Substitution: find the indefinite integral.

1. $\int \pi \cos \pi x dx$

2. $\int x \sin x^2 dx$

3. $\int \frac{\sin x}{\cos^3 x} dx$

4. $\int \sqrt{\tan x} \sec^2 x dx$

Find a equation for the function that has the given derivative and whose graph passes through the given point.

5. $f'(x) = \sec^2(2x) \quad \left(\frac{\pi}{2}, 2\right)$

Find the indefinite integral by the method in Ex 5 in the book.

6. $\int x\sqrt{3x+1}dx$

Evaluate the definite integral. Check using your calculator

7. $\int_{-2}^4 x^2(x^3+8)^2 dx$

8. $\int_1^2 (x-1)\sqrt{2-x} dx$

Evaluate the integral using the properties of even and odd functions as an aid.

Integration of Even and Odd Functions:

Let f be integrable on the closed interval $[-a, a]$.

1. If f is an even function, then
$$\int_{-a}^a f(x)dx = 2 \int_0^a f(x)dx$$

2. If f is an odd function, then
$$\int_{-a}^a f(x)dx = 0$$

Evaluate the integral using the properties of even and odd functions as an aid.

9.
$$\int_{-2}^2 x(x^2 + 1)^3 dx$$