

Simplify

- $e^{16}e^{-10} = e^6$
- $5e^{-2x} = \frac{5}{e^{2x}}$
- $(2e)^{-3} = \frac{1}{(2e)^3} = \frac{1}{8e^3}$

Warm Up

4. You deposit \$15,000 in an account earning 3.7% interest compounded for 5 years. How much will you have if its

- Compounded monthly  $\$18043.14$
- Continuously compounded  $\$18048.28$

5. The car you bought for \$5500 depreciates 10% each year. How much will it be worth in 3 years?

$$y = a(1-r)^t$$

$$y = 5500(1-.1)^3$$

$$y = \$4009.50$$

Apr 1-12:23 PM

# 7.4 Logarithms

IF  $2^2 = 4$  and  $2^3 = 8$ ,

THEN  $2^x = 6$ ?

How do I algebraically get the unknown when its an exponent?

Feb 20-9:45 AM

## 7.4 Logarithmic functions

**Logarithm Defined:**

"the exponent that indicates the power to which a base number is raised to produce a given number <the logarithm of 100 to the base 10 is 2>"

In simpler terms - a logarithm is an exponent

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Base<sup>Exponent</sup> = Answer → Exponent Form

$$2^3 = 8$$

$\log_{\text{Base}} \text{Answer} = \text{Exponent}$  → Logarithmic Form

$$\log_2 8 = 3$$

We say "log base two of 8 equals 3"

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FIRST JOB is re-writing equations from exponential to logarithmic form and back again

Logarithmic Form	Exponential Form
a. $\log_2 8 = 3$	$2^3 = 8$
b. $\log_4 1 = 0$	$4^0 = 1$
c. $\log_{12} 12 = 1$	$12^1 = 12$
d. $\log_{1/4} 4 = -1$	$(\frac{1}{4})^{-1} = 4$

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Rewrite the equation in exponential form.

- $\log_3 81 = 4$  →  $3^4 = 81$
- $\log_7 7 = 1$  →  $7^1 = 7$
- $\log_{14} 1 = 0$  →  $14^0 = 1$
- $\log_{1/2} 32 = -5$  →  $(\frac{1}{2})^{-5} = 32$

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2nd JOB is evaluating logarithmic functions without a calculator

Ex.  $\log_4 64 = x$     *add*  $4^x = 64$      $x=3$   
 $\log_{12} 12 = x$     *rewrite*  $12^x = 12$      $x=1$   
 $\log_2 32 = x$      $2^x = 32$      $x=5$   
 $\log_{1/5} 125 = x$      $(\frac{1}{5})^x = 125$      $x=-3$   
 $\log_{36} 6 = x$      $36^x = 6$      $x = \frac{1}{2}$   
 $\sqrt[3]{x} = x^{\frac{1}{3}}$

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3rd job Practice Evaluating with a calculator

(make sure you know how to with a calculator as well)

Calculator assumes a base of 10

$\log 17 = 1.2304$

$\log 2 = .301$

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Some simple facts.

COMMON LOGARITHM is a logarithm with base 10

$\log_{10} x = \log x$

*if theres no base  $\Rightarrow$  assume 10*

NATURAL LOGARITHM is a logarithm with base "e"

$\log_e x = \ln x$

Find ln on your calculator

$\ln 22 = 3.09$

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4th Job Finding/Using INVERSES of Functions

The logarithmic function

$g(x) = \log_b x$

is the INVERSE of the exponential function

$f(x) = b^x$

$g(x) = \log_b x$      $f(x) = b^x$     *poor*

$g(f(x)) = \log_b b^x = x$     *answer is exp*

$f(g(x)) = b^{\log_b x} = x$     *answer is answer on exponent*

HW

$\log_5 125^x =$   
 $\log_5 5^{3x} = 3x$

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If Exponential and Logarithmic Functions are Inverses to one another ... we can use this to help us solve.

$g(x) = \log_b x$   
 $f(x) = b^x$

$g(f(x)) = \log_b b^x = x$

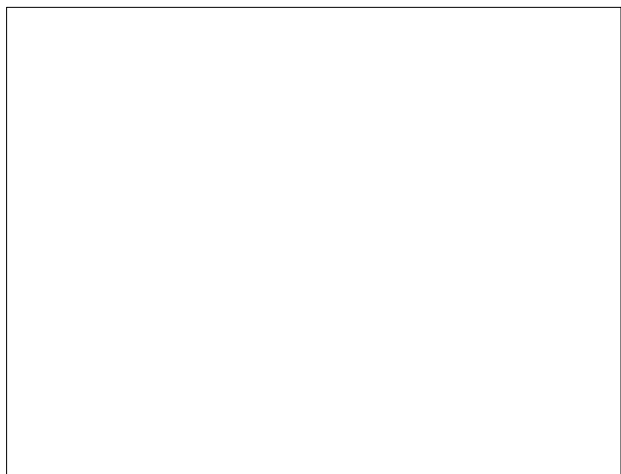
$f(g(x)) = b^{\log_b x} = x$

Mar 31-12:45 PM

Your book is not your friend in the section.

It is your enemy.

Mar 31-12:42 PM



Apr 27-8:52 AM

Find the inverse:

*Switch forms*

1st Switch x & y then switch forms

1.  $y = 6^x$   
 $x = 6^y$

$\log_6 y = x$

2.  $y = \ln(x+3)$        $e^x = y + 3$   
 $x = \ln(y+3)$        $e^x - 3 = y$

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HW Pg 503

#3-6

#8-19

#24,25

properties #28-31 **no stress**

Apr 6-11:44 AM