

Jan 11-11:30 AM

*** EXTENDED RESPONSE** A passenger in an airplane sees two towns directly to the left of the plane.

a. What is the distance d from the airplane to the first town?
 b. What is the horizontal distance x from the airplane to the first town?
 c. What is the distance y between the two towns? Explain the process you used to find your answer.

$90 - 25 = 65^\circ$

$25k$ 65° d

$\tan 65 = \frac{x}{25000}$
 $\cos 65 = \frac{25000}{d}$

$d = 59,157.6$
 $x = 53,612.67$

$65 + 10 = 75^\circ$

$25k$ 75° $x+y$ z

$\tan 75 = \frac{z}{25000}$
 $z = 93,301.27$

$y = z - x$
 $y = 39,688.5$

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Draw an angle with the given measure in standard position.

a) $\frac{2\pi}{7}$ $\frac{735\pi}{7}$ **$\frac{105\pi}{7}$**
 b) $\frac{11\pi}{6}$ $\frac{2\pi}{6}$ **$\frac{14\pi}{6}$**
 c) $-\pi$ $4\frac{2\pi}{3}$ **$\frac{8\pi}{3}$**
 d) $\frac{5\pi}{3}$

e) 135° f) 290° g) 220° h) -110°

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Coterminals

Add or subtract 360 or 2π **Need Common denominator!**

Find 1 positive and 1 negative coterminal angle for each angle listed.

a) $\frac{2\pi}{7}$ $2\pi = \frac{14\pi}{7}$ $\frac{2\pi}{7} + \frac{14\pi}{7} = \frac{16\pi}{7}$ $\frac{2\pi}{7} - \frac{14\pi}{7} = \frac{-12\pi}{7}$
 b) $\frac{11\pi}{6}$ $2\pi = \frac{12\pi}{6}$ $\frac{11\pi}{6} + \frac{12\pi}{6} = \frac{23\pi}{6}$ $\frac{11\pi}{6} - \frac{12\pi}{6} = \frac{-\pi}{6}$
 c) $-\pi$ $2\pi = \frac{8\pi}{4}$ $-\pi + \frac{8\pi}{4} = \frac{6\pi}{4}$ $-\pi - \frac{8\pi}{4} = \frac{-10\pi}{4}$
 d) $\frac{5\pi}{3}$

e) 135° f) 290° g) 220° h) -110°

$135 + 360 = 495^\circ$ $290 + 360 = 650^\circ$ $220 + 360 = 580^\circ$
 $135 - 360 = -225^\circ$ $290 - 360 = -70^\circ$ $220 - 360 = -140^\circ$

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Convert between degrees and radians

Multiply by $\frac{180}{\pi}$ or $\frac{\pi}{180}$ and REDUCE

a) $\frac{2\pi}{7}$ b) $\frac{11\pi}{6}$ $\frac{630}{180} = 3.5$ $\frac{11\pi}{6} \cdot 3.5 = \frac{385\pi}{6}$ $\frac{385\pi}{6} - 62\pi = \frac{11\pi}{6}$ **$\frac{11\pi}{6}$**
 c) $-\pi$ $\frac{4 \cdot 45\pi}{\pi} = 180$ $-\pi + 180 = 179$ **179°**
 d) $\frac{5\pi}{3}$

e) 135° f) $290^\circ \cdot \frac{\pi}{180} = \frac{29\pi}{18}$ **$\frac{29\pi}{18}$**
 g) $220^\circ \cdot \frac{\pi}{180} = \frac{11\pi}{9}$ **$\frac{11\pi}{9}$**
 h) -110°

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Extra Credit

On back

① 2 special triangles with angle measurements & side lengths

② List 6 trig ratios and the shortcut to remember the first 3.

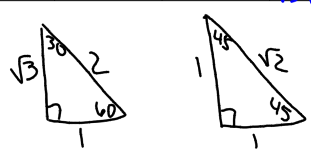
③ solve for c

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Fill in the chart using your 2 special triangles

	30°	45°	60°
Radians			
sin θ	$\frac{1}{2}$	$\frac{\sqrt{2}}{2} = \frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$
cos θ	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$
tan θ	$\frac{1}{\sqrt{3}} = \frac{\sqrt{3}}{3}$	1	$\sqrt{3}$
csc θ	2	$\sqrt{2}$	$\frac{2}{\sqrt{3}} = \frac{2\sqrt{3}}{3}$
sec θ	$\frac{2}{\sqrt{3}} = \frac{2\sqrt{3}}{3}$	$\sqrt{2}$	2
cot θ	$\sqrt{3}$	1	$\frac{1}{\sqrt{3}} = \frac{\sqrt{3}}{3}$

\sin
 \cos
 \tan

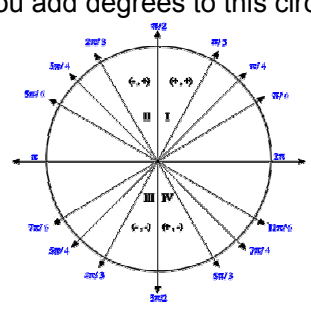


\sin
 \cos
 \tan

\csc
 \sec
 \cot

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Can you add degrees to this circle...



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Homework questions...

LETS DLT!

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So far.

- Right Triangle Trig - listing ratios, solving side lengths, WP
- 3 new trig functions - csc, sec, cot
- Graphing angles in degrees
- Radians - learning, graphing
- Coterminal angles in degrees and radians
- Converting angles between degrees and radians

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1st job - Evaluate 6 trig functions given point

EXAMPLE: You are given a point...on a circle

Let $(-4, 3)$ be a point on the terminal side of an angle θ in standard position. Evaluate the six trigonometric functions of θ .

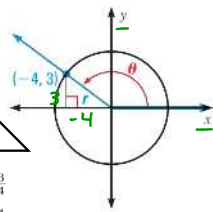
Solution

Use the Pythagorean theorem to find the value of r .

$$r = \sqrt{x^2 + y^2} = \sqrt{(-4)^2 + 3^2} = \sqrt{25} = 5$$

Using $x = -4$, $y = 3$, and $r = 5$, you can write the following:

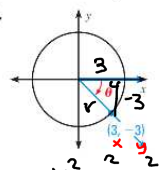
$\sin \theta = \frac{y}{r} = \frac{3}{5}$	$\cos \theta = \frac{x}{r} = -\frac{4}{5}$	$\tan \theta = \frac{y}{x} = -\frac{3}{4}$
$\csc \theta = \frac{r}{y} = \frac{5}{3}$	$\sec \theta = \frac{r}{x} = -\frac{5}{4}$	$\cot \theta = \frac{x}{y} = -\frac{4}{3}$

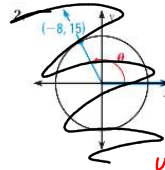


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YOU DO THE WORK!!!!

Evaluate the six trigonometric functions of θ .

1. 

2. 

$x^2 + y^2 = r^2$
 $3^2 + (-3)^2 = r^2$
 $9 + 9 = r^2$
 $\sqrt{r} = \sqrt{18}$
 $r = 3\sqrt{2}$

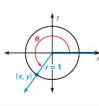
$\sin \theta = \frac{y}{r} = \frac{4}{3\sqrt{2}} = \frac{-1}{\sqrt{2}} = \frac{-\sqrt{2}}{2}$
 $\cos \theta = \frac{x}{r} = \frac{3}{3\sqrt{2}} = \frac{1}{\sqrt{2}} = \frac{\sqrt{2}}{2}$
 $\tan \theta = \frac{y}{x} = \frac{-3}{3} = -1$

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2nd job UNIT CIRCLE - same concept...what if the radius is 1...

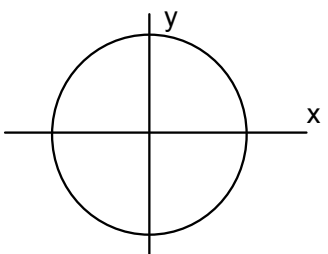
$\sin\theta = y$ $\csc\theta = 1/y$
 $\cos\theta = x$ $\sec\theta = 1/x$
 $\tan\theta = y/x$ $\cot\theta = x/y$

KEY CONCEPT For Your Notebook
The Unit Circle
 The circle $x^2 + y^2 = 1$, which has center (0, 0) and radius 1, is called the **unit circle**. The values of $\sin \theta$ and $\cos \theta$ are simply the y-coordinate and x-coordinate, respectively, of the point where the terminal side of θ intersects the unit circle.
 $\sin \theta = \frac{y}{r} = \frac{y}{1} = y$ $\cos \theta = \frac{x}{r} = \frac{x}{1} = x$



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The unit circle gives us our axis trig values
 FOUR CASES OF QUADRANTAL ANGLES:



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List 6 trig functions for...

a) $\frac{\pi}{2}$ (0,1) b) π (-1,0)

(x,y) (cos, sin)

(0,1) (0,-1) (1,0) (-1,0)

$\sin\theta = \frac{y}{r} = \frac{1}{1} = 1$
 $\cos\theta = \frac{x}{r} = \frac{0}{1} = 0$
 $\tan\theta = \frac{y}{x} = \frac{1}{0} = \text{und}$
 $\csc\theta = \frac{1}{\sin\theta} = \frac{1}{1} = 1$
 $\sec\theta = \frac{1}{\cos\theta} = \frac{1}{0} = \text{und}$
 $\cot\theta = \frac{\cos\theta}{\sin\theta} = \frac{0}{1} = 0$

c) -90° d) 0°

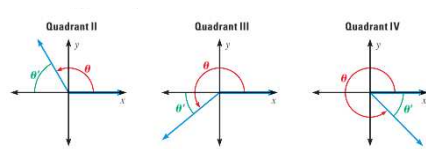
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REFERENCE ANGLES

KEY CONCEPT For Your Notebook
 A reference angle is an acute angle formed by the terminal side of the angle and the x-axis.

symbol

The Books Way



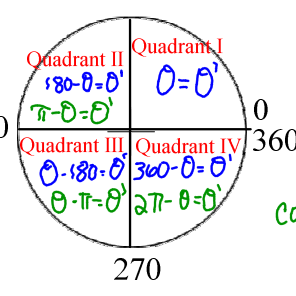
Quadrant II: Degrees: $\theta' = 180^\circ - \theta$, Radians: $\theta' = \pi - \theta$
 Quadrant III: Degrees: $\theta' = \theta - 180^\circ$, Radians: $\theta' = \theta - \pi$
 Quadrant IV: Degrees: $\theta' = 360^\circ - \theta$, Radians: $\theta' = 2\pi - \theta$

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To Find REFERENCE ANGLES

Mrs B Way

$\theta' = \text{reference angle}$



Quadrant I: $0 = \theta'$
 Quadrant II: $180 - \theta = \theta'$
 Quadrant III: $\theta - 180 = \theta'$
 Quadrant IV: $360 - \theta = \theta'$

Common denominator to add/subtract fractions

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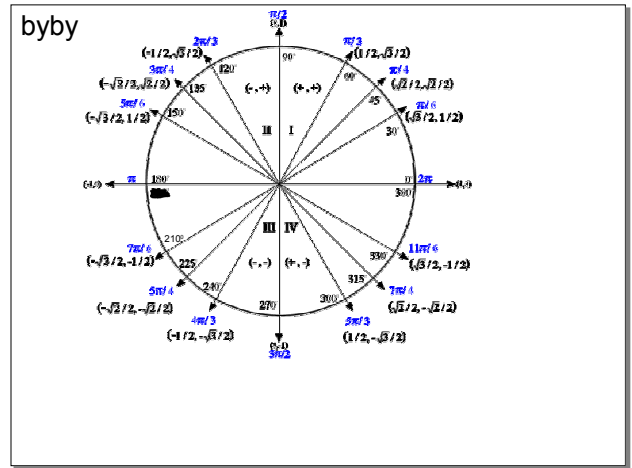
3rd Job HINT: DRAW IT!
 FIND THE REFERENCE ANGLE FOR THE FOLLOWING:
 In degrees...

- 325°
- 99°
- 22°

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In Radians
 4. $5\pi/6$ 5. $-4\pi/5$

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Chp 13.3
 GENERAL DEFINITIONS OF TRIGONOMETRIC FUNCTIONS

KEY CONCEPT *For Your Notebook*

General Definitions of Trigonometric Functions

Let θ be an angle in standard position, and let (x, y) be the point where the terminal side of θ intersects the circle $x^2 + y^2 = r^2$. The six trigonometric functions of θ are defined as follows:

$\sin \theta = \frac{y}{r}$

$\cos \theta = \frac{x}{r}$

$\tan \theta = \frac{y}{x}, x \neq 0$

$\csc \theta = \frac{r}{y}, y \neq 0$

$\sec \theta = \frac{r}{x}, x \neq 0$

$\cot \theta = \frac{x}{y}, y \neq 0$

These functions are sometimes called *circular functions*.

Job 1

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