

Mr. Jones lives 50 miles away from you. You both leave home at 5:00 and drive toward each other.



Mr. Jones travels at 35 mph, and you drive at 40 mph. At what time will you pass Mr. Jones on the road?



GIVEN THE TRAFFIC GROUND HERE AT 5:00, WHO KNOWS?



I ALWAYS CATCH THESE TRICK QUESTIONS.



10.4-10.5 Applications of Matrices and Determinants

Let's look at:

$$\left. \begin{array}{l} b_2(a_1x + b_1y = c_1) \\ b_1(a_2x + b_2y = c_2) \end{array} \right\} x = \frac{c_1 b_2 - c_2 b_1}{a_1 b_2 - a_2 b_1}$$

solve for x

$$\begin{array}{r} a_1 b_2 x + \cancel{b_1 b_2 y} = c_1 b_2 \\ - a_2 b_1 x + \cancel{b_1 b_2 y} = c_2 b_1 \\ \hline a_1 b_2 x - a_2 b_1 x = c_1 b_2 - c_2 b_1 \\ x(a_1 b_2 - a_2 b_1) = c_1 b_2 - c_2 b_1 \end{array}$$

Let's look at:

$$a_1x + b_1y = c_1$$

$$a_2x + b_2y = c_2$$

solve for y

$$y = \frac{a_2 b_1 - b_2 c_1}{a_1 b_2 - a_2 b_1}$$

Cramer's Rule

$$x = \frac{\begin{vmatrix} c_1 & b_1 \\ c_2 & b_2 \end{vmatrix}}{\begin{vmatrix} a_1 & b_1 \\ a_2 & b_2 \end{vmatrix}}$$

$$y = \frac{\begin{vmatrix} a_1 & c_1 \\ a_2 & c_2 \end{vmatrix}}{\begin{vmatrix} a_1 & b_1 \\ a_2 & b_2 \end{vmatrix}}$$

Use Cramer's Rule to solve:

$$4x - 2y = 10$$

$$3x - 5y = 11$$

$$(2, -1)$$

$$x = \frac{\begin{vmatrix} 10 & -2 \\ 11 & -5 \end{vmatrix}}{\begin{vmatrix} 4 & -2 \\ 3 & -5 \end{vmatrix}} = \frac{-28}{-14}$$

$$y = \frac{\begin{vmatrix} 4 & 10 \\ 3 & 11 \end{vmatrix}}{\begin{vmatrix} 4 & -2 \\ 3 & -5 \end{vmatrix}} = \frac{14}{-14}$$

Use Cramer's Rule to solve:

$$-7x + 11y = -1$$

$$3x - 9y = 9$$

$$2x + y - 3z = 15$$

$$4x - y + 2z = -9$$

$$-2x + 2y + z = 6$$

$$x = \frac{\begin{vmatrix} 15 & 1 & -3 \\ -9 & -1 & 2 \\ 6 & 2 & 1 \end{vmatrix}}{\begin{vmatrix} 2 & 1 & -3 \\ 4 & -1 & 2 \\ -2 & 2 & 1 \end{vmatrix}}$$

$$y = \frac{\begin{vmatrix} 2 & 15 & -3 \\ 4 & -9 & 2 \\ -2 & 6 & 1 \end{vmatrix}}{\begin{vmatrix} 2 & 1 & -3 \\ 4 & -1 & 2 \\ -2 & 2 & 1 \end{vmatrix}}$$

→ same

$$z = \frac{\begin{vmatrix} 2 & 1 & 15 \\ 4 & -1 & -9 \\ -2 & 2 & 6 \end{vmatrix}}{\begin{vmatrix} 2 & 1 & -3 \\ 4 & -1 & 2 \\ -2 & 2 & 1 \end{vmatrix}}$$

→ same

Area of a Triangle:

The area of a triangle with vertices (x_1, y_1) , (x_2, y_2) , and (x_3, y_3) is:

$$\text{Area} = \pm \frac{1}{2} \begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix}$$

Find the area of a triangle
whose vertices are:
 $(1,0)$, $(2,2)$, $(4,3)$

Cryptography: a **cryptogram** is a message written according to a secret code.

MEET ME MONDAY

[13 5 5][20 0 13][5 0 13][15 14 4][1 25 0

$$\begin{bmatrix} 1 & -2 & 2 \\ -1 & 1 & 3 \\ 1 & -1 & -4 \end{bmatrix}$$